



### Nonlinear Macromodeling of Amplifiers and Applications to Filter Design.

### By Edgar Sanchez-Sinencio

Thanks to Heng Zhang for part of the material

### **OP AMP MACROMODELS**

Systems containing a significant number of Op Amps can take a lot of time of simulation when Op Amps are described at the transistor level. For instance a 5<sup>th</sup> order filter might involve 7 Op Amps and if each Op Amps contains say 12 to 15 transistors, the SPICE analysis of a circuit containing 60 to 75 Transistors can be too long and tricky in particular for time domain simulations. Therefore the use of a macromodel representing the Op Amp behavior reduces the simulation time and the complexity of the analysis.

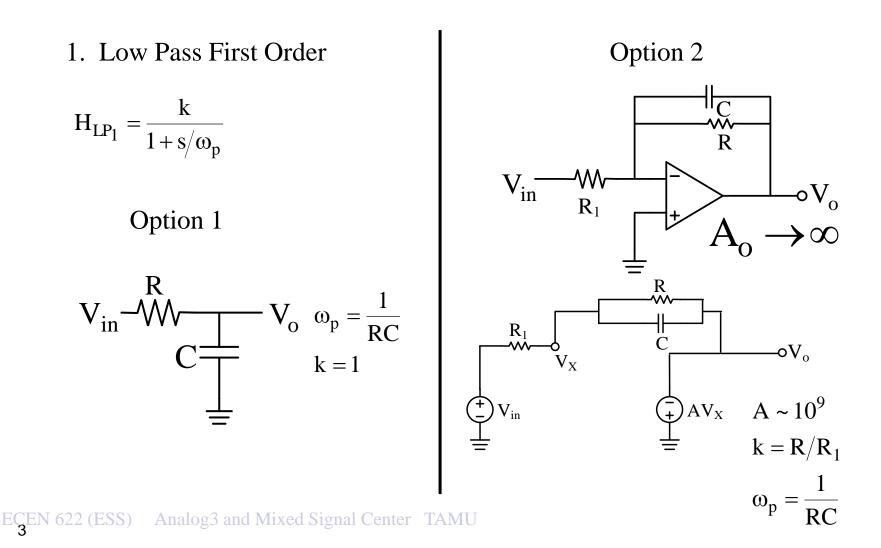
The simplicity of the analysis of Op Amps containing macromodels is because macromodels can be implemented using SPICE primitive components. Some examples of macromodels are discussed next.

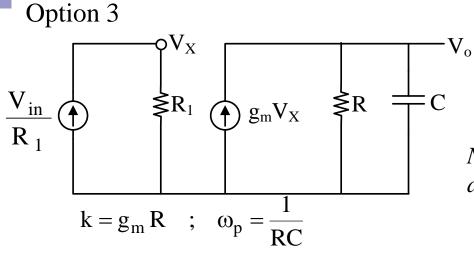
http://www.analog.com/static/imported-files/application\_notes/48136144500269408631801016AN138.pdf

http://www.national.com/analog/amplifiers/spice\_models

ECEN 622(ESS) Analog and Mixed Signal Center TAMU

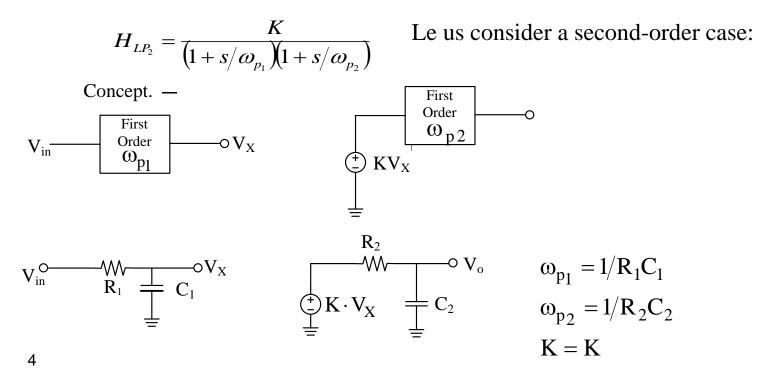
#### FUNDAMENTAL ON MACROMODELING USING ONLY PRIMITIVE SPICE COMPONENTS

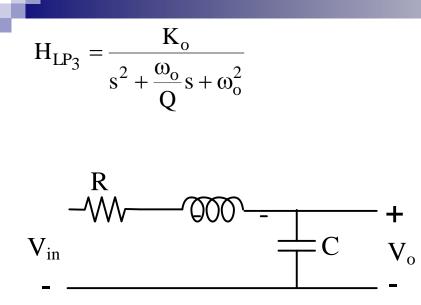




Note.- If you need to isolate the output use a final VCVS with a gain of one

2. Higher Order Low Pass





$$K_{o} = 1/LC \quad ; \quad H_{LP_{3}}(0) = 1$$
$$\omega_{o}^{2} = 1/LC$$
$$\frac{\omega_{o}}{Q} = \frac{R}{L}$$

Resonator (one zero, two complex poles)

$$k = 1/LC$$
  

$$\omega_z = R/L$$
  

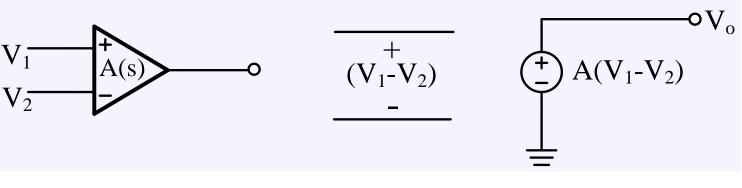
$$\omega_o^2 = 1/LC$$
  

$$\frac{\omega_o}{Q} = 1/RC$$

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#### ECEN 622(ESS)

#### **Op Amps (VCVS) Linear Modeling**

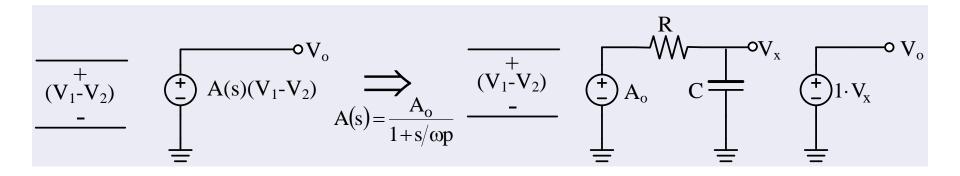


**Op Amp Symbol** 

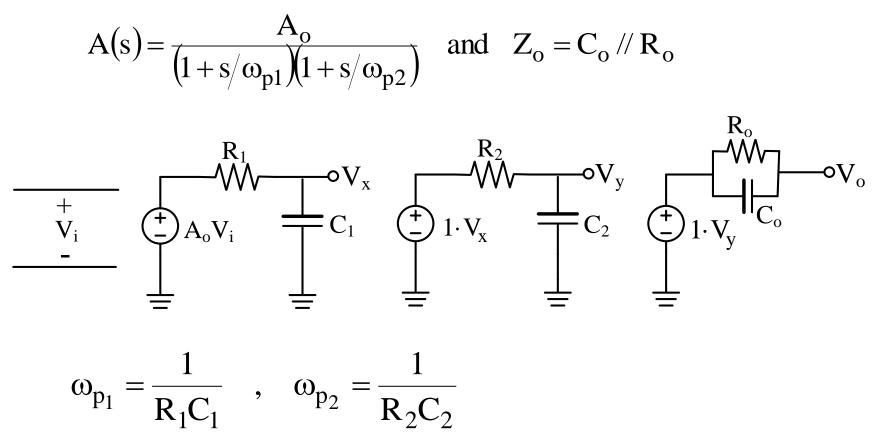
1. Quasi-Ideal Model, A>>10<sup>3</sup>

TAMU-AMSC

- 2. For finite DC Gain, Make  $A=A_{o}$
- 3. Frequency Dependent Gain (one dominant pole)

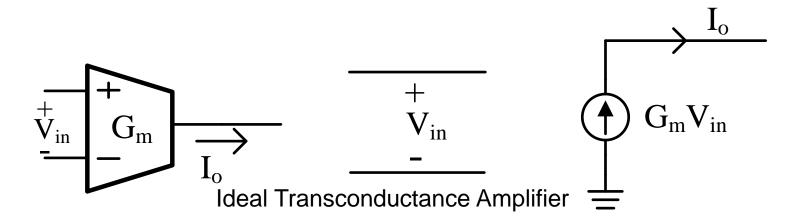


4. Frequency dependent gain with two poles:

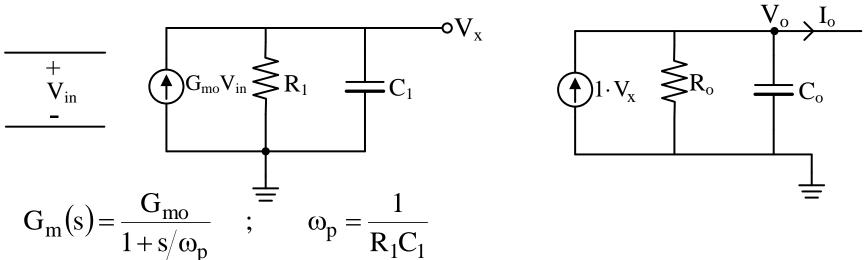


 $A_o$  is the open loop DC gain. The output impedance consists of  $R_o//C_o$ .

#### Transconductance Amplifier (VCIS) Linear Modeling



**Frequency dependent G**<sub>m</sub> and fine output impedance

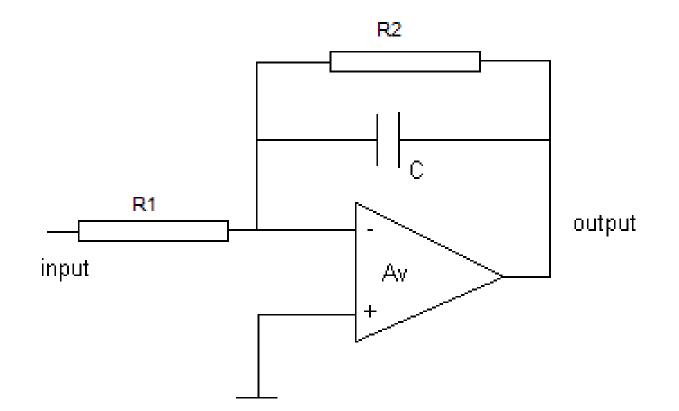


 $Z_o$  consists of a large output resistor ( $R_o$ ) and a small output capacitance ( $C_o$ ).

### Active RC Filter Design with Nonlinear Opamp Macromodel

- Design a two stage Miller CMOS Op Amp in 0.35 µm and propose a macromodel containing up to the seventh-harmonic component
- Compare actual transistor model versus the proposed non-linear macromodel
- Use both macromodel and transistor level to design a LP filter with H(o) =10dB, f<sub>3dB</sub>=5 MHz
- Result comparison

### 1<sup>st</sup> order Active-RC LP filter



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# Filter transfer function with Ideal Opamp

$$H_{LP,ideal}(s) = -\frac{R_2}{R_1} \frac{1}{(1+sR_2C)}$$
(1)

$$H(o) = 10dB \rightarrow \frac{R_2}{R_1} = 10dB = 3.16$$
 (2)

$$f_{3dB} = 5 \text{ MHz} \rightarrow \frac{1}{R_2 C} = 6.28 * 5 \text{M} = 31.4 \text{ Mrad}$$
 (3)

Choose R1, R2 and C from equations (1) ~ (3). To minimize loading effect, R2 should be large enough. Here we choose R2 =  $31.6k\Omega$ , R1 =  $10k\Omega$ , and C = 1pF.

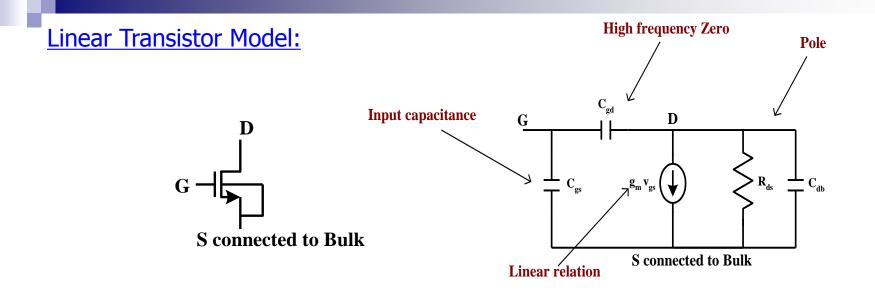
### Filter transfer function with finite Opamp gain and GBW

One pole approximation for Opamp Modeling: Av = GB/s.(it holds when GBW >> f<sub>3dB</sub> and Av(0) >>1)

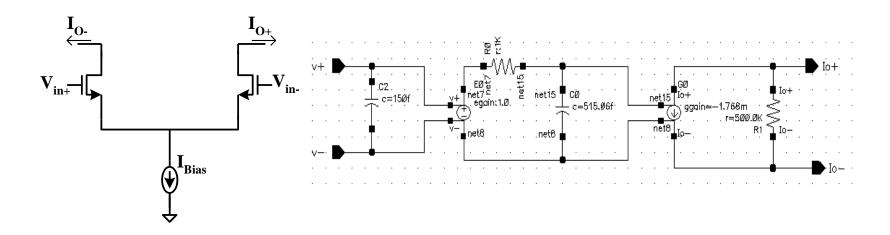
$$H_{LP,nonideal}(s) = \frac{-R_2}{R_1(1 + \frac{s}{GB})(1 + sR_2C) + \frac{s}{GB}R_2}$$

A two stage Miller Op amp is designed. GBW is chosen ~20 times the f<sub>3dB</sub> to minimize the finite GBW effect; GBW = 100MHz is also easy to achieve in 0.35µm CMOS technology. Non-Linear Model for a source-degenerated OTA

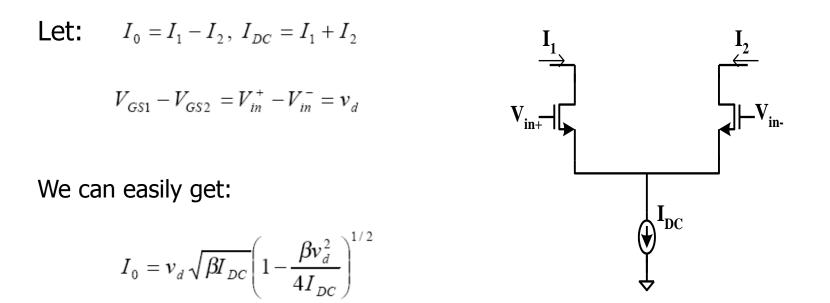
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#### Linear OTA model:



#### Non-Linear OTA model:



Which can be expanded to:  $I_0 = \alpha_1 v_d + \alpha_3 v_d^3 + O(v_d^5)$ 

To determine Odd Harmonic effects for an ideal OTA !!

#### How to Extract the Coefficients:

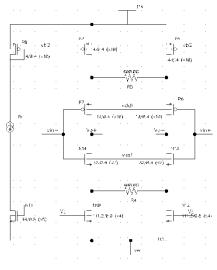
Generally if we have:  $i_{out} = a_0 + a_1 v_d + a_2 v_d^2 + a_3 v_d^3$ 

We can extract the coefficients by differentiation, where:

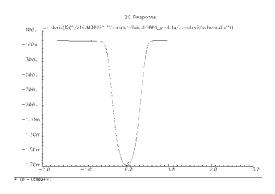
At 
$$v_d = 0$$
,  $i_{out} = a_o$   $\frac{d}{dv_d}i_{out} = a_1$   $\frac{d^2}{dv_d^2}i_{out} = 2a_2$   $\frac{d^3}{dv_d^3}i_{out} = 6a_3$ 

- By Sweeping the input voltage and integrating the output current, we can these coefficients.
- a<sub>2</sub> is ideally zero.
- Getting the first <u>3</u> coefficients only is a valid approximation.

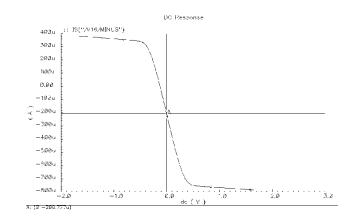
#### A source degenerated OTA as an example:



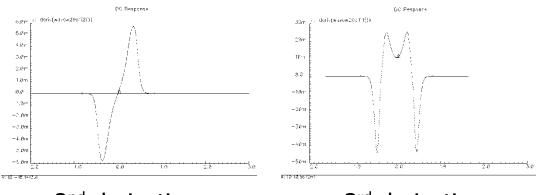
OTA



1<sup>st</sup> derivative



### Output current of one branch versus input differential voltage.



2<sup>nd</sup> derivative

3<sup>rd</sup> derivative

#### Coefficients:

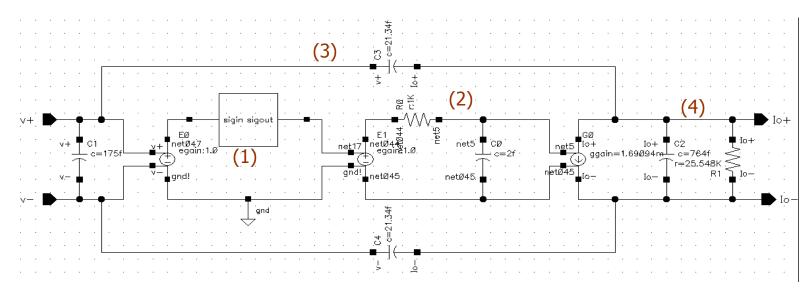
 $a_0 = 206.777 \ \mu A$  $a_1 = 1.69094 \ m A/v$  $a_2 = 9.07 \ \mu A/v2$  $a_3 = -1.764 \ m A/v3$ 

File						Help	15	
Curve3 - ( Curve2 - (	: deriv(deriv(deriv(I: deriv(deriv(IS("/VO, deriv(IS("/VO/PLUS") IS("/VO/PLUS")	/PLUS" "/scratch/	faisal/HW4_prob1	lc/spectreS/schem	natic")))			
Curve table:	X value	Curve4	Curve3	Curve2	Curve1			
M1 (anchor)	0	10.583547602m	-19, 19775648u	-1.690939075m	-206. 7681432u			

The accuracy of these numbers depends on the number of points used in the DC sweep.

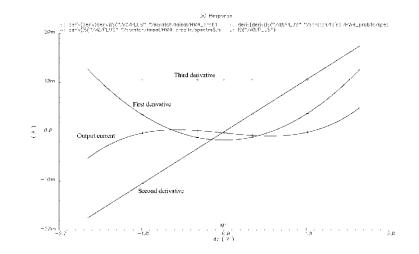
By taking more points, even harmonics reduce to zero.

#### Macromodel used:



- 1. Non-linear transfer function.
- 2. non-dominant pole .
- 3. Feed-forward path leads to Right half plane zero. ( $C_{gd}$  of the driver trans.)
- 4. Output Resistance and Load Capacitance.

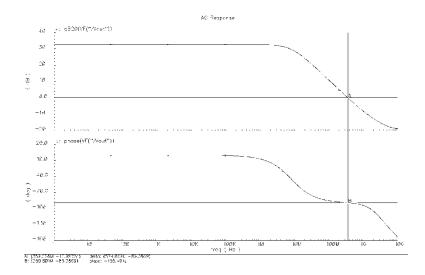
#### DC sweep of Macromodel:

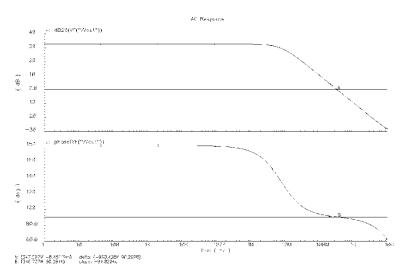


	Transistor level	Macro-model	Percentage of error
a <sub>0</sub> (µA)	206.777	206.768	4.3 m %
a <sub>1</sub> (mA/V)	1.69094	1.69094	0
$a_2 (\mu A/V^2)$	9.07	9.5988	5.5 %
a <sub>3</sub> (mA/V <sup>3</sup> )	-1.764	-1.7639	5.66 m %

Changes due to measurement accuracy and number of points

#### AC response comparison:



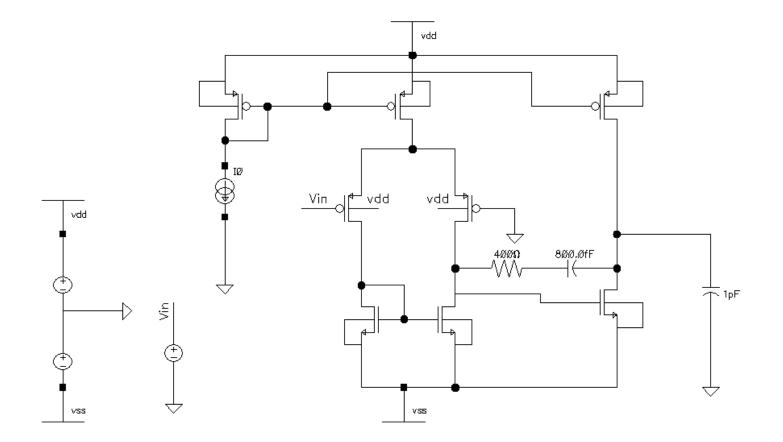


#### Transistor level

#### Macro-model

	Transistor level	Macro-model	Percentage of error
DC gain	32.8 dB	32.8 dB	0
w₀	359.226 MHz	347.69 MHz	3.3 %
Phase margin	90.62 <sup>0</sup>	89.7 <sup>0</sup>	1.015 %

### Two stage Miller Amplifier Design

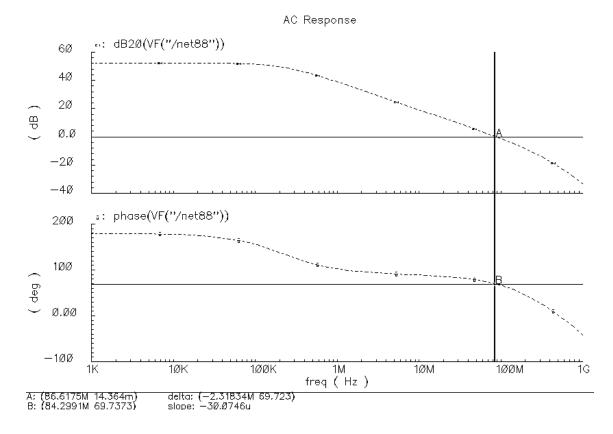


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# **Opamp Design parameters**

Power	278uA @ 3V		
1 <sup>st</sup> Stage	PMOS(W/L)	30u/0.4u	
	NMOS(W/L)	15u/0.4u	
2 <sup>nd</sup> Stage	PMOS(W/L)	120u/0.4u	
	NMOS(W/L)	60u/0.4u	
Miller	Cm	800fF	
Compensation	Rm	400 Ω	

# **OPAMP Frequency response**

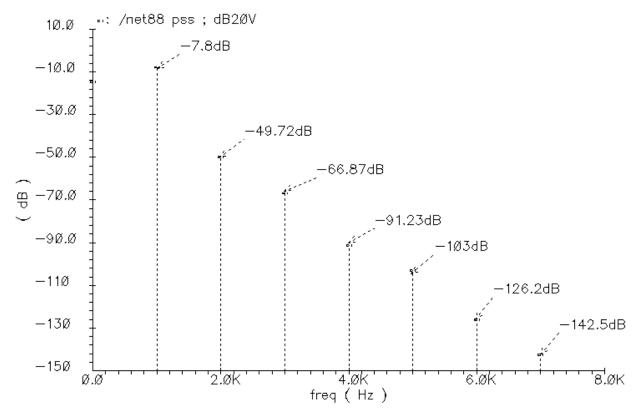


DC Gain: 53 dB, GBW: 86.6 MHz, phase margin: 69.7 deg.
 Dominant pole:154KHz, Second pole: 197MHz

### **Output Spectrum of Open loop OPAMP**

#### 1mVpp input @ 1KHz (THD= -49.2dB)





$$V_{out} = a_o + a_1 v_d + a_2 v_d^2 + a_3 v_d^3 + a_4 v_d^4 + a_5 v_d^5 + a_6 v_d^6 + a_7 v_d^7$$
  

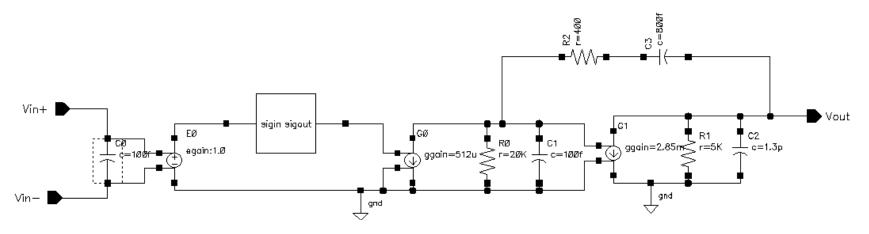
$$a_1 \sim a_7 \text{ can be extracted from PSS simulation results:}$$
  

$$a_1 = DC \text{ gain} = 450$$

$$HD_{2} = \frac{a_{2}A}{2a_{1}} = 41.92dB \quad \Rightarrow a_{2} = 2934$$
$$HD_{3} = \frac{a_{3}A^{2}}{4a_{1}} = 59.1dB \quad \Rightarrow a_{3} = 2.16e6$$

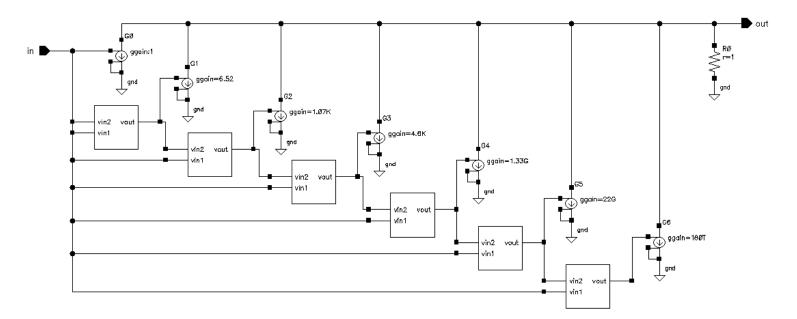
Similarly, we can obtain:  $a_4 = 6e7$ ,  $a_5 = 5.6e11$ ,  $a_6 = 1e13$ ,  $a_7 = 7e16$ 

# **Opamp Macro model**



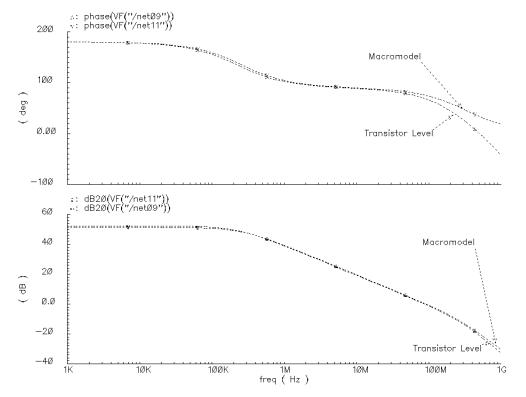
- Modeled: input capacitance, two poles, one RHP zero, nonlinearity, finite output resistance, and capacitance
- Nonlinearity model should be placed before the poles to avoid poles multiplication

# **Nonlinearity Model**



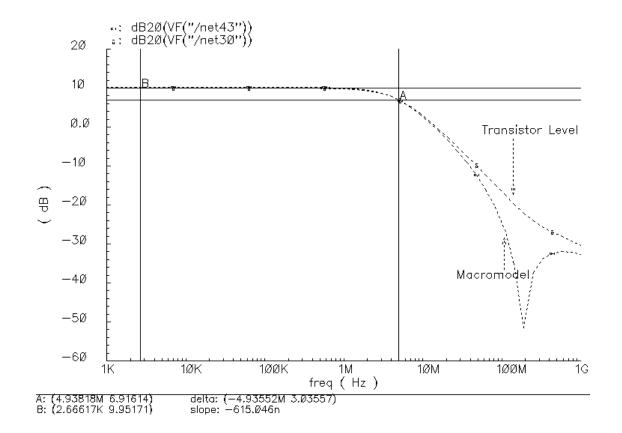
- uses mixer blocks to generate nonlinear terms
- model up to 7<sup>th</sup> order non-linearity
- set each VCCS Gain as the nonlinear coefficients.
- set the gain for 1<sup>st</sup> VCCS = gm1 = 512uA/V, gain for 2<sup>nd</sup> VCCS = gm2 = 2.85mA/V, and scale all the nonlinear coefficients derived above by a<sub>1</sub>.

### Opamp AC response: Transistor-level vs. Macromodel

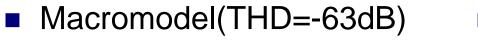


- Macro-model mimic the transistor level very well at frequencies below 10MHz
- discrepancy at higher frequency due to the higher order poles and zeros not modeled in the Macromodel

# Filter AC response: Transistor-level vs. Macromodel

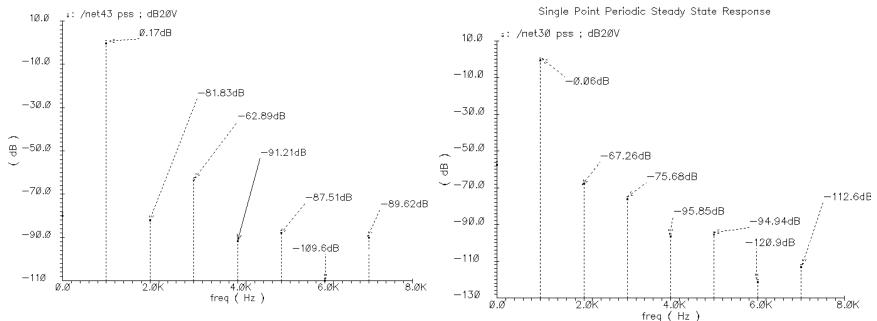


### Output Spectrum (0dBm input @ 1KHz)



Single Point Periodic Steady State Response

# Transistor Level(THD = -66.4dB)



# **Performance Comparison**

Table I. Open loop Opamp Performance Comparison

	Transistor Level	Macro-model
-3dB BW	154KHz	180KHz
GBW	86.6MHz	90MHz
DC Gain	53 dB	51.3 dB
Phase Margin	69.7 degree	74.9 degree
THD: -50dBm @ 1KHz	-49.2 dB	-49.6 dB

#### Table II. LPF Performance Comparison

	Transistor Level	Macro-model
BW of LPF	4.9MHz	4.86MHz
DC Gain of LPF	9.95 dB	10.19 dB
THD: 0dBm @ 1KHz	-66.4 dB	-63dB

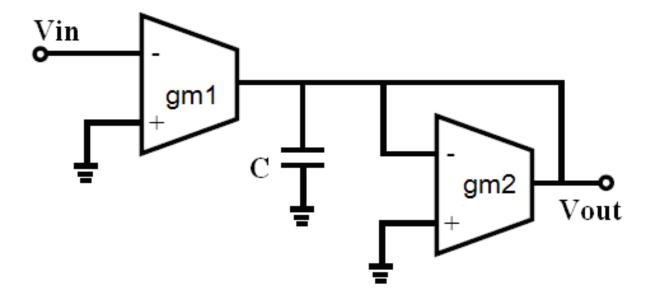
### **Observation**

- THD of the LPF at 0dBm input is better than that of the open loop Opamp with a small input at -50dBm. This is because OPAMP gain is ~50 dB, when configured as a LPF, OPAMP input is attenuated by the feedback loop-> better linearity.
- when keep increasing the input amplitude, the THD of the transistor-level degrades dramatically. This is because large swing activates more nonlinearity and even cause transistors operating out of saturation region; however, the THD of Macro-model doesn't reflect this because we didn't implement the limiter block.

# Gm-C Filter Design with Nonlinear Opamp Macromodel

- Use a three current mirror Transconductance Amplifier.
- Compare actual transistor model versus the non-linear macromodel
- Use both macromodel and transistor level to design a LP filter with H(o) =10dB, f<sub>3dB</sub>=5 MHz
- Result Comparison

### 1<sup>st</sup> order Gm-C LP filter



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### Filter transfer function

With Ideal OTA:

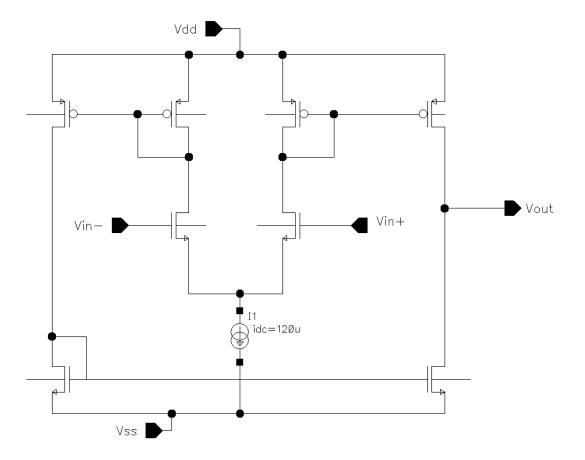
$$H(s)_{ideal} = -\frac{g_{m1}}{g_{m2}} \frac{1}{1 + sC / g_{m2}}$$

H(o) = 10dB 
$$\rightarrow \frac{g_{m1}}{g_{m2}}$$
 = 10dB = 3.16

$$f_{3dB} = 5 \text{ MHz} \rightarrow \frac{g_{m2}}{C} = 6.28*5 \text{ M} = 31.4 \text{ Mrad}$$

Output resistance of gm1 should be >> 1/gm2 Choose C = 4pF,  $\rightarrow$  gm2 = 0.126mA/V, gm1 = 0.4mA/V

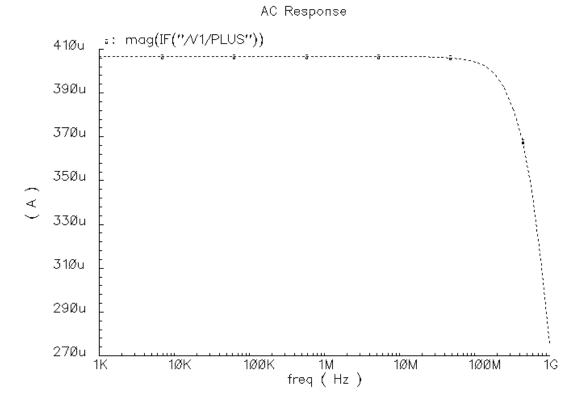
### Three Current mirrors OTA Design



# **OTA Design parameters**

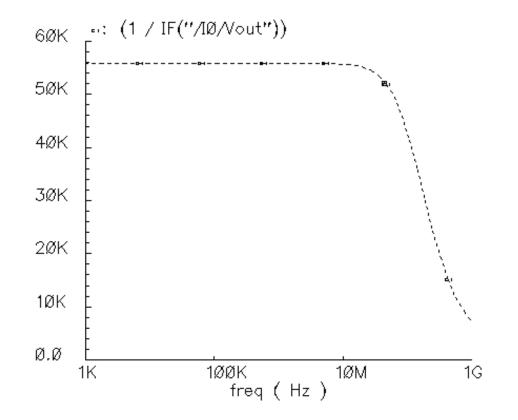
Power	240uA @ <u>+</u> 1.5V
Input NMOS	4u/0.6u
PMOS current mirror	12u/0.4u
NMOS current mirror	1u/0.4u

## AC simulation of Gm: Transistor Level



gm = 0.4mA/V, which is our desired value its frequency response is good enough for a LPF with 5MHz cutoff frequency

#### **OTA Output resistance:** Transistor Level



output resistance of the OTA >>1/gm2

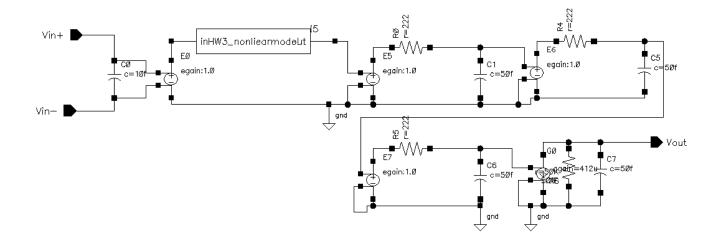
#### Gm-C LPF Output spectrum: Transistor level

∴: /net7 pss ; dB2ØV Ø.ØØ -1.15dB -1Ø.Ø -2Ø.Ø -27.38dB -3Ø.Ø -4Ø.Ø -52.56dB Щ -5Ø.Ø -6Ø.57dB -6Ø.Ø -7Ø.Ø -8Ø.Ø -9Ø.Ø -1ØØ '2.øk 'в.øк ø.ø '4.ØK '6.'øk freq (Hz)

Single Point Periodic Steady State Response

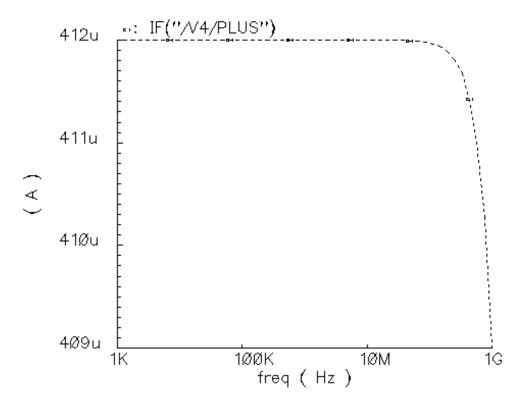
THD = -26dB for 0dBm input@1kHz

# **OTA Macro model**

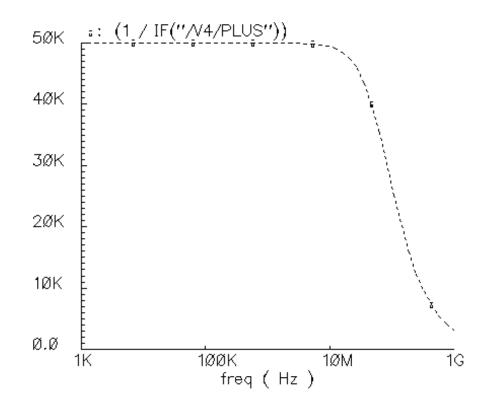


- Since the internal poles and zeros are at much higher frequency than 5MHz, only the important ones are included in the macro-model
- Nonlinearity model is the same as the Opamp in Active-RC filter

### AC simulation of Gm: Macro-model

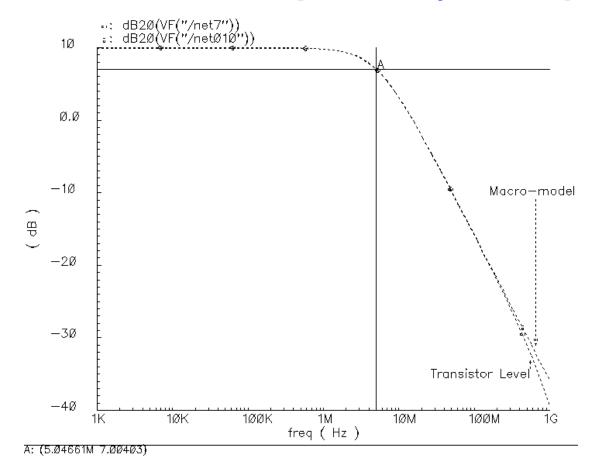


#### **OTA Output resistance:** Macro-model



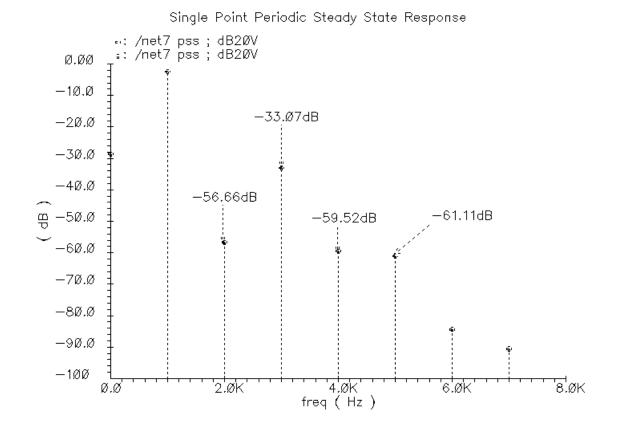
output resistance of the OTA >>1/gm2

## **Gm-C LPF Frequency response**



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#### Gm-C LPF Output spectrum: Macromodel



THD = -33dB for 0dBm input@1kHz

## **Performance Comparison**

 $\sqrt{Hz}$ 

Table I. Gm-C Filter Performance Comparison

	Transistor Level	Macro-model
Gm	409uA/V	412uA/V
BW of LPF	5.05MHz	5.05MHz
DC Gain of LPF	10 dB	10 dB
THD: 0dBm @ 1KHz	-26 dB	-33dB

Table II. Comparison between Transistor Level Active-RC and Gm-C LPF

	Active RC	Gm-C
DC gain	9.95dB	10dB
BW	4.9MHz	5.05MHz
THD: 0dBm @ 1KHz	-66.4 dB	-26 dB
Noise Level	0.048µV/@1kHz	0.05µV/@1kHz
Power	0.83mW	0.72mW

## Discussion

- With comparable DC gain, BW, Noise level and Power consumption, Gm-C filter has much worse linearity than Active RC because:
  - □ Active RC: feedback configuration improves linearity;
  - Gm-C filter: open loop operation, the gm stage sees large signal swing, thus linearization technique is needed, which adds power consumption.

Active RC is preferable for low frequency applications if linearity is a key issue