## ECEN721: Optical Interconnects Circuits and Systems Spring 2024

Lecture 5: Transimpedance Amplifiers (TIAs)



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## Announcements

- Exam 1 Mar 7
  - In class
  - One double-sided 8.5x11 notes page allowed
  - Bring your calculator
  - Covers through Lecture 6
- Reading
  - Sackinger Chapter 5
  - Razavi Chapter 4

# Agenda

- Optical Receiver Overview
- Transimpedance Amplifiers
  - Common-Gate TIAs
  - Feedback TIAs
  - Common-Gate & Feedback TIA Combinations
  - Differential TIAs
- Integrating Optical Receivers
- Equalization in Optical Front-Ends

# **Optical Receiver Technology**

- Photodetectors convert optical power into current
  - p-i-n photodiodes
  - Waveguide Ge photodetectors
- Electrical amplifiers then convert the photocurrent into a voltage signal
  - Transimpedance amplifiers
  - Limiting amplifiers
  - Integrating optical receiver



# Transimpedance Amplifier (TIA)





Also expressed in units of dB $\Omega$  by  $20\log(|Z_T|)$ 

- Key design objectives
  - High transimpedance gain
  - Low input resistance for high bandwidth and efficient gain
- For large input currents, the TIA gain can compress and pulse-width distortion/jitter can result 5

# Maximum Currents



- Input Overload Current
  - The maximum peak-to-peak input current for which we can achieve the desired BER
  - Assuming high extinction ratio  $i_{ovl}^{pp} = 2R\overline{P}_{ovl}$
- Maximum Input Current for Linear Operation
  - Often quantified by the current level for a certain gain compression (1dB)

$$i_{lin}^{pp} < i_{ovl}^{pp}$$

## **Resistive Front-End**



 Direct trade-offs between transimpedance, bandwidth, and noise performance

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## Common-Gate TIA



 Input resistance (input bandwidth) and transimpedance are decoupled

### **Common-Gate TIA Frequency Response**



 Often the input pole may dominate due to large photodiode capacitance (100 – 500fF)

# Common-Gate TIA Noise



Neglecting transistor  $r_0$ :

$$\overline{V_{n,out}^2} = \left(\overline{I_{n,M2}^2} + \overline{I_{n,RD}^2}\right)R_D^2 = 4kT\left(\frac{2}{3}g_{m2} + \frac{1}{R_D}\right)R_D^2 \quad \left(\frac{\mathbf{V}^2}{\mathbf{Hz}}\right)$$
$$\overline{I_{n,in}^2} = 4kT\left(\frac{2}{3}g_{m2} + \frac{1}{R_D}\right) \quad \left(\frac{\mathbf{A}^2}{\mathbf{Hz}}\right)$$

- Both the bias current source and RD contribute to the input noise current
- RD can be increased to reduce noise, but voltage headroom can limit this
- Common-gate TIAs are generally not for low-noise applications
- However, they are relatively simple to design with high stability

# Regulated Cascode (RGC) TIA

- Input transistor gm is boosted by commonsource amplifier gain, resulting in reduced input resistance
- Requires additional voltage headroom
- Increased input-referred noise from the commonsource stage

#### [Park ESSCIRC 2000]



# CMOS 20GHz TIA

- An additional commongate stage in the feedback provides further gm-boosting and even lower input resistance
- Shunt-peaking inductors provide bandwidth extension at zero power cost, but very large area cost



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# Feedback TIA w/ Ideal Amplifier



- Input bandwidth is extended by the factor A+1
- Transimpedance is approximately R<sub>F</sub>
- Can make R<sub>F</sub> large without worrying about voltage headroom considerations

### Feedback TIA w/ Finite Bandwidth Amplifier



With Finite Bandwidth Amplifier :

 $Q = \frac{\sqrt{(A+1)R_F C_T T_A}}{R_T C_T + T_A}$ 

 $R_{in} = \frac{R_F}{A+1}$ 

 Finite bandwidth amplifier modifies the transimpedance transfer function to a secondorder low-pass function

### Feedback TIA w/ Finite Bandwidth Amplifier

- Non-zero amplifier time constant can actually increase TIA bandwidth!!
- However, can result in peaking in frequency domain and overshoot/ringing in time domain
- Often either a Butterworth (Q=1/sqrt(2)) or Bessel response (Q=1/sqrt(3)) is used
  - Butterworth gives maximally flat frequency response
  - Bessel gives maximally flat group-• delay





# Feedback TIA Transimpedance Limit

If we assume a Butterworth response for mazimally flat frequency response :

$$Q = \frac{1}{\sqrt{2}} \implies \omega_A = \frac{1}{T_A} = \frac{2A}{R_F C_T}$$

For a Butterworth response :

$$\omega_{3\text{dB}} = \omega_0 = \sqrt{\frac{(A+1)\omega_A}{R_F C_T}} = \frac{\sqrt{(A+1)2A}}{R_F C_T} \approx \sqrt{2} \text{ times larger than } T_A = 0 \text{ case of } \frac{A+1}{R_F C_T}$$

Plugging  $R_T = \frac{A}{A+1}R_F$  into above expression yields the maximum possible  $R_T$  for a given bandwidth

$$\sqrt{\frac{(A+1)\omega_A}{\left(\frac{A+1}{A}\right)R_TC_T}} \ge \omega_{3dB}$$
Maximum  $R_T \le \frac{A\omega_A}{C_T}$ 

[Mohan JSSC 2000]

- Maximum R<sub>T</sub> proportional to amp gain-bandwidth product
- If amp GBW is limited by technology f<sub>T</sub>, then in order to increase bandwidth, R<sub>T</sub> must decrease quadratically!

## Feedback TIA



Assuming that the source follower has an ideal gain of 1

 $A = g_{m1}R_D$  $R_T = \frac{g_{m1}R_D}{1 + g_{m1}R_D}R_F$  $R_{in} = \frac{R_F}{1 + g_{m1}R_D}$  $R_{out} = \frac{1}{g_{m2}(1 + g_{m1}R_D)}$ 

 As power supply voltages drop, there is not much headroom left for RD and the amplifier gain degrades

# **CMOS Inverter-Based Feedback TIA**



- CMOS inverter-based TIAs allow for reduced voltage headroom operation
- Cascaded inverter-gm + TIA stage provide additional voltage gain
- Low-bandwidth feedback loop sets the amplifier output common-mode level

# **Input-Referred Noise Current**



- TIA noise is modeled with an input-referred noise current source that reproduces the output TIA output noise when passed through an ideal noiseless TIA
- This noise source will depend on the source impedance, which is determined mostly by the photodetector capacitance

### Input-Referred Noise Current Spectrum



- Input-referred noise current spectrum typically consists of uniform, high-frequency f<sup>2</sup>, & lowfrequency 1/f components
- To compare TIAs, we need to see this noise graph out to ~2X the TIA bandwidth
  - Recall the noise bandwidth tables

# Input-Referred RMS Noise Current

 The input-referred rms noise current can be calculated by dividing the rms output noise voltage by the TIA's midband transimpedance value

$$i_{n,TIA}^{rms} = \frac{1}{R_T} \sqrt{\int_0^{>2BW} |Z_T(f)|^2 I_{n,TIA}^2(f) df}$$

- If we integrate the output noise, the upper bound isn't too critical. Often this is infinity for derivations, or 2X the TIA bandwidth in simulation
- This rms current sets the TIA's electrical sensitivity

$$i_{sens}^{pp} = 2Qi_{n,TIA}^{rms}$$

 To determine the total optical receiver sensitivity, we need to consider the detector noise and responsivity

#### Averaged Input-Referred Noise Current Density

• TIA noise performance can also be quantified by the averaged input-referred noise current density

$$i_{n,TIA}^{avg} = \frac{i_{n,TIA}^{rms}}{\sqrt{BW_{3dB}}}$$

This quantity has units of 
$$\left(\frac{pA}{\sqrt{Hz}}\right)$$
.

Note, this is different than averaging the input - referred noise spectrum,  $I_{n,TIA}^2(f)$  over the TIA bandwidth.

### FET Feedback TIA Input-Referred Noise Current Spectrum



 The feedback resistor and amplifier front-end noise components determine the input-referred noise current spectrum

$$I_{n,TIA}^2(f) = I_{n,res}^2(f) + I_{n,front}^2(f)$$

• The feedback resistor component is uniform with frequency  $I_{n,res}^{2}(f) = \frac{4kT}{R_{T}}$ 

### FET Feedback TIA Input-Referred Noise Current Spectrum



Gate current-induced shot noise

$$I_{n,G}^2 = 2qI_G$$

This is typically small for CMOS designs

FET channel noise

$$I_{n,D}^2 = 4kT\Gamma g_m$$

 $\Gamma$  is the channel noise factor, typically 0.7 - 3 depending on the process.

## Input-Referring the FET Channel Noise

To do this, we could calculate

$$\frac{i_{n,TIA}}{i_{n,D}} = \frac{\left(\frac{v_{out}}{i_{n,D}}\right)}{Z_T}$$

But it is easier (and equivalent) to ground the output and calculate

$$\left(\frac{i_{n,D}}{i_{n,TIA}}\right)^{-1}$$
$$i_{n,D} = g_m v_{n,TIA} = \frac{g_m i_{n,TIA}}{sC_T + \frac{1}{R_F}} = \frac{g_m R_F}{1 + sR_F C_T} i_{n,TIA}$$



where  $C_T = C_D + C_I$ , the summation of the detector and amplifier input capacitance.

$$\left(\frac{i_{n,D}}{i_{n,TIA}}\right)^{-1} = \frac{1 + sR_FC_T}{g_mR_F}$$

Using this high - pass transfer function, the input - referred FET channel noise is

$$I_{n,front,D}^{2}(f) = \frac{1 + (2\pi f R_{F} C_{T})^{2}}{(g_{m} R_{F})^{2}} \cdot 4kT\Gamma g_{m}$$
  
=  $4kT\Gamma \left(\frac{1}{g_{m} R_{F}^{2}}\right) + 4kT\Gamma \left(\frac{(2\pi C_{T})^{2}}{g_{m}}\right) f^{2}$  Uniform and f<sup>2</sup> component!

#### Total Input-Referred FET Feedback TIA Noise



 Note that the TIA input-referred noise current spectrum begins to rise at a frequency lower than the TIA bandwidth

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# Common-Gate & Feedback TIA



- Recall that the feedback TIA stability depends on the ratio of the input pole (set by C<sub>D</sub>) and the amplifier pole
  - Large variation in C<sub>D</sub> can degrade amplifier stability
- Common-gate input stage isolates C<sub>D</sub> from input amplifier capacitance, allowing for a stable response with a variety of different photodetectors
- Transimpedance is still approximately R<sub>F</sub>A/(1+A)

# BJT Common-Base & Feedback TIA



- Transformer-based negative feedback boosts gm with low power and noise overhead
- Input series peaking inductor isolates the photodetector capacitance from the TIA input capacitance
- High frequency techniques allow for 26GHz bandwidth with group delay variation less than 19ps

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# **Differential TIAs**

- Differential circuits have superior immunity to power supply/substrate noise
- A differential TIA output allows easy use of common differential main/limiting amplifiers
  - This comes at the cost of higher noise and power
- How to get a differential output with a single-ended photocurrent input?
  - Two common approaches, based on the amount of capacitance applied at the negative input



# Balanced TIA

 A balanced TIA design attempts to match the capacitance of the two differential inputs

 $C_X \approx C_D$ 

- This provides the best power supply/substrate noise immunity, as the noise transfer functions are similar
- Due to double the circuitry, the input-referred rms noise current is increased by sqrt(2)



Assuming an high BW amplifier and  $C_T = C_D + C_I$ 

$$Z_T(s) = \frac{v_{OP} - v_{ON}}{i_i} = \frac{\left(\frac{A}{A+1}\right)R_F}{1 + \frac{sC_TR_F}{A+1}}$$

Same transfer function as the single - ended design

# **Pseudo-Differential TIA**

- A pseudo-differential TIA design uses a very large capacitor at the negative input, such that it can be approximated as an AC ground  $C_X \rightarrow \infty$
- While not good to reject power supply/substrate noise, it does provide significant filtering of the R<sub>F</sub>' noise
- The differential transimpedance is approximately doubled relative to the single-ended case



Assuming an high BW amplifier

and  $C_T = C_D + C_I$ 

$$Z_T(s) = \frac{v_{OP} - v_{ON}}{i_i} = \frac{\left(\frac{2A}{A+2}\right)R_F}{1 + \frac{sC_TR_F}{\frac{A}{2} + 1}}$$

# Offset Control

- Due to the single-ended photodetector signal, the differential output signal swings from 0 to V<sub>ppd</sub>, which can limit the dynamic range
- Adding offset control circuitry can allow for an output swing of ±V<sub>ppd</sub>/2



## **Differential Shunt Feedback TIA**



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# **Optical RX Scaling Issues**



# Integrating Receiver Block Diagram



# **Demultiplexing Receiver**



- Demultiplexing with multiple clock phases allows higher data rate
  - Data Rate = #Clock Phases x Clock Frequency
  - Gives sense-amp time to resolve data
  - Allows continuous data resolution

# **1V Modified Integrating Receiver**



#### **Differential Buffer**

- Fixes sense-amp common-mode input for improved speed and offset performance
- © Reduces kickback charge
- ⊗ Cost of extra power and noise
- Input Range = 0.6 1.1V

## **Receiver Sensitivity Analysis**



# Integrating Receiver Sensitivity

#### • Test Conditions

- 8B/10B data patterns (variance of 6 bits)
- Long runlength data (variance of 10 bits)
- BER < 10<sup>-10</sup>



## Integrating RX with Dynamic Threshold



## Integrating RX with Dynamic Threshold



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# Low-BW TIA & CTLE Front-End



- Improved sensitivity is possible by increasing the first stage feedback resistor, resulting in a high-gain low-bandwidth TIA
- The resultant ISI is cancelled by a subsequent CTLE

## Active CTLE Example



# Low-BW TIA & CTLE Front-End



# Low-BW TIA & CTLE Front-End

#### [Li JSSC 2014]



#### 25Gb/s Eye Diagram







# Low-BW TIA & DFE RX



- In a similar manner, a high-gain low-bandwidth TIA is utilized
- The resultant ISI is cancelled by a subsequent 1-tap loopunrolled DFE

# DFE Example

- If only DFE equalization, DFE tap coefficients should equal the unequalized channel pulse response values  $[a_1 a_2 \dots a_n]$
- With other equalization, DFE tap coefficients should equal the pre-DFE pulse response values
  - DFE provides flexibility in the optimization of other equalizer circuits
  - i.e., you can optimize a TX equalizer without caring about the ISI terms that the DFE will take care of





 $[w_1 w_2] = [a_1 a_2]$ 

6Gb/s Eye - Refined BP Channel w/ RX DFE Eq



# Low-BW TIA & DFE RX



- As RF is increased, the main cursor increases and the SNR improves is ISI is cancelled by a DFE
- Large performance benefit with a low-complexity 1-tap DFE

# Low-BW TIA & DFE RX

#### [Ozkaya JSSC 2017]



- Self-referenced TIA is used for differential generation
- Actual 64Gb/s pulse response has a significant pre-cursor ISI tap, which requires a 2-tap TX FFE

#### 64Gb/s Pulse Response & Timing Margin



# Next Time

Main/Limiting Amplifiers